

# Multiplying Integers

*Unit Topic* : **Multiplying and Dividing Rational Numbers**

*Grade level* : 7<sup>th</sup>

*Presenter* : Dung Le

# Lecture Objectives

*STUDENTS ARE ABLE TO:*

- **REPRESENT A MULTIPLICATION PROBLEM OF THE FORM  $P \times Q$ , WHERE  $P$  OR  $Q$  IS A POSITIVE OR NEGATIVE INTEGER, BY WRITING A PHRASE AND DRAWING AN INTEGER TILES PICTURE TO REPRESENT THE PROBLEM.**
- **CALCULATE THE PRODUCT OF THE MULTIPLICATION PROBLEM USING INTEGER TILES.**
- **RECOGNIZE THE SIGN OF THE PRODUCT OF TWO INTEGERS WHEN THE TWO INTEGERS HAVE THE SAME OR DIFFERENT SIGNS.**

# Math Content Standards

## **CCSS.MATH.CONTENT.7.NS.A.2**

APPLY AND EXTEND PREVIOUS UNDERSTANDINGS OF MULTIPLICATION AND DIVISION AND OF FRACTIONS TO MULTIPLY AND DIVIDE RATIONAL NUMBERS.

### **CCSS.MATH.CONTENT.7.NS.A.2.A**

UNDERSTAND THAT MULTIPLICATION IS EXTENDED FROM FRACTIONS TO RATIONAL NUMBERS BY REQUIRING THAT OPERATIONS CONTINUE TO SATISFY THE PROPERTIES OF OPERATIONS, PARTICULARLY THE DISTRIBUTIVE PROPERTY, LEADING TO PRODUCTS SUCH AS  $(-1)(-1) = 1$  AND THE RULES FOR MULTIPLYING SIGNED NUMBERS. INTERPRET PRODUCTS OF RATIONAL NUMBERS BY DESCRIBING REAL-WORLD CONTEXTS.

### **CCSS.MATH.CONTENT.7.NS.A.2.C**

APPLY PROPERTIES OF OPERATIONS AS STRATEGIES TO MULTIPLY AND DIVIDE RATIONAL NUMBERS.

# How to Present The Multiplication Problem below?


$$3 \times 5$$

Yes/No Question

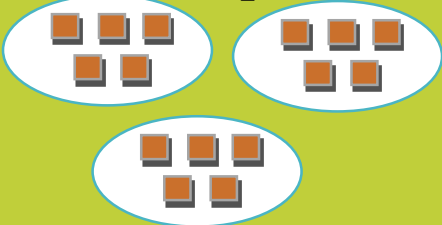
Yes or No?  $3 + 5$

Yes or No? Repeated Addition  
 $5 + 5 + 5$

Yes or No? An array with 3 rows and 5 columns



Yes or No? 3 groups of 5



# MORE: How to Present Other Multiplication Problems?

## Multiplication Problems

$$3 \times -5$$

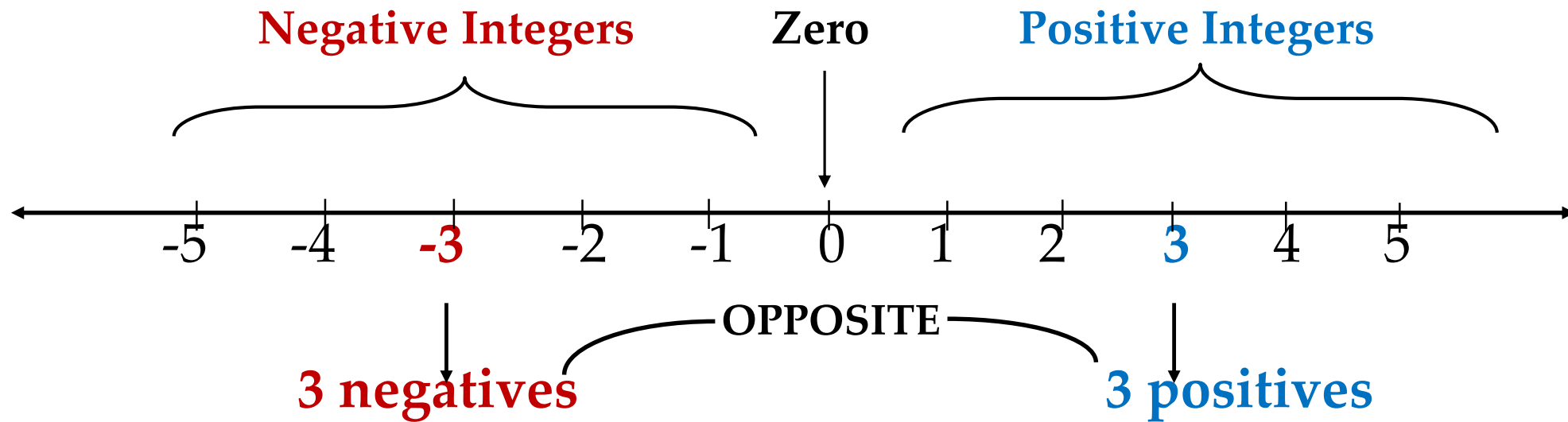
$$-3 \times 5$$

$$-3 \times -5$$



# Review: Positive and Negative Integers

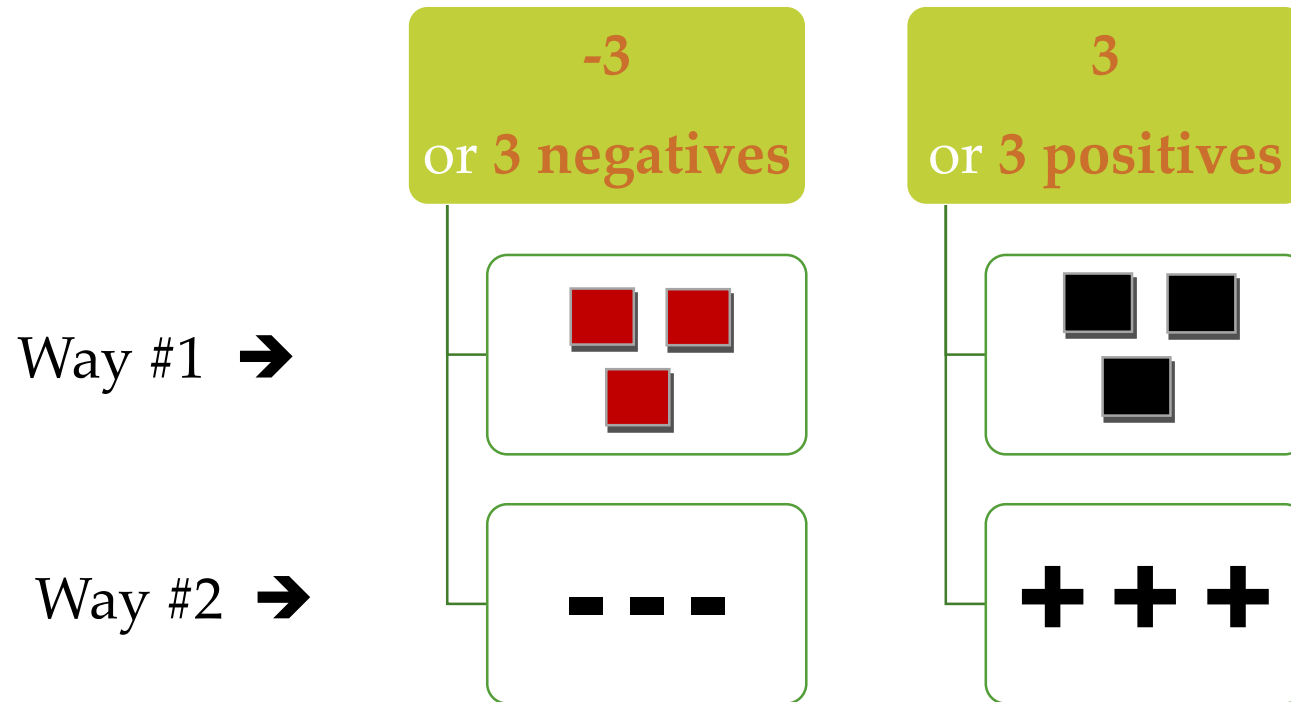
## A Number Line



*The opposite of 3 negatives is 3 positives*

*The opposite of 3 positives is 3 negatives*

# Using Virtual Integer Tiles to Represent Integers







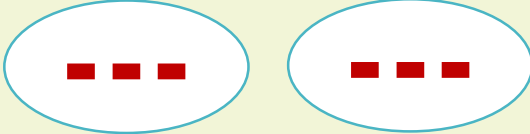
*Note:* You can color the virtual integer tiles  $+$  and  $-$ , e.g.,  $+$  and  $-$

## NOW YOU TRY: Use Integers Tiles to Represent Some Integers

REQUEST	IMPLEMENTATION
Use integer tiles to present 7 negatives	
Use integer tiles to present 11 positives	
Use integer tiles to present the <u>opposite</u> of 7 negatives	
Use integer tiles to present the <u>opposite</u> of 11 positives	
Use integer tiles to present two groups of 3 negatives (two groups, each group has 3 negatives)	



# EXAMPLES: Use Integers Tiles to Represent Some Integers

REQUEST	IMPLEMENTATION
Use integer tiles to present 7 negatives	
Use integer tiles to present 11 positives	
Use integer tiles to present the <u>opposite</u> of 7 negatives	
Use integer tiles to present the <u>opposite</u> of 11 positives	
Use integer tiles to present two groups of 3 negatives (two groups, each group has 3 negatives)	

# NOW YOU TRY: Use Integer Tiles to Represent $3 \times 5$

Fill out the blanks

## Multiplication

How many groups?

$3 \times 5$

How many in each group?

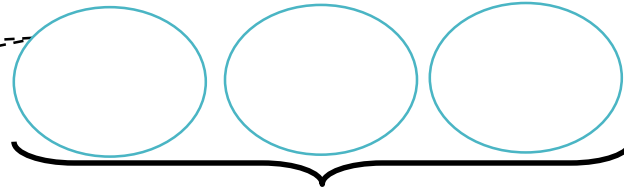
=

The product

Write: \_\_\_\_\_ groups of \_\_\_\_\_ positives

Draw: Use integer tiles to represent the problem

Fill up what are inside each group



\_\_\_\_\_ groups

The product (the total from the groups) = \_\_\_\_\_

# WHAT WE FOUND: Use Integer Tiles to Represent $3 \times 5$

## Multiplication

3  
groups

$3 \times 5$

5 positives  
in each group

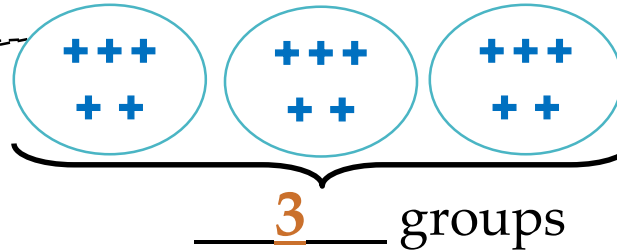
= 15

The product

Write: 3 groups of 5 positives





Draw: Use integer tiles to represent the problem

Fill up what are inside  
each group




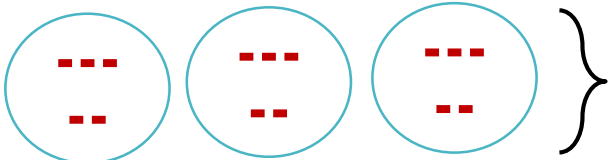


The product (the total from the groups): 15 positives




# The 4 TYPICAL PROBLEMS of Multiplying Integers

<b>PROBLEM</b> 	<i>Write</i> 	 <b>Draw: Use integer tiles to represent the problem</b>	<b>The product</b>
$3 \times 5$	3 groups of 4 positives		<b>15</b>
$3 \times -5$			
$-3 \times 5$			
$-3 \times -5$			




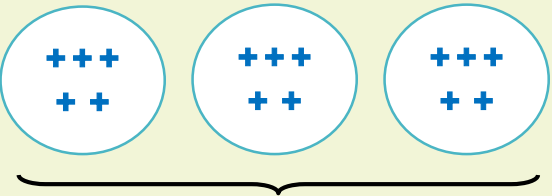
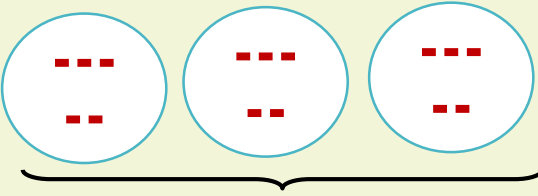
# Solve Problem 2: $3 \times -5$

<b>PROBLEM</b> 	<i>Write</i> 	 <b>Draw: Use integer tiles to represent the problem</b>	<b>The product</b>
$3 \times 5$			
$3 \times -5$	3 groups of 5 negatives	 <p>The total:  <math>\rightarrow -15</math></p>	$-15$
$-3 \times 5$			
$-3 \times -5$			




# NOW YOU TRY: Solve $2x - 7$

<b>PROBLEM</b> 	<i>Write</i> 	 <b>Draw: Use integer tiles to represent the problem</b>	<b>The product</b>
$2x - 7$			

# Solve Problem 3: $-3 \times 5$




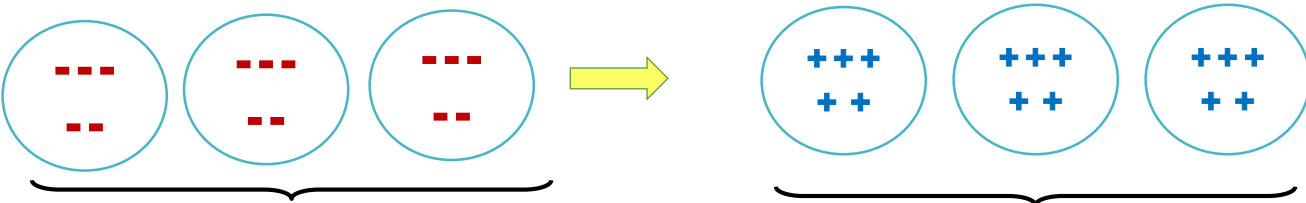
<b>PROBLEM</b> 	<i>Write</i> 	 <b>Draw: Use integer tiles to represent the problem</b>	<b>The product</b>
$3 \times 5$			
$3 \times -5$			
$-3 \times 5$	<p>The <b>OPPOSITE</b> of 3 groups of 5 positives</p>	<p><u>3 groups of 5 positives</u></p>  <p>→</p> <p><u>The OPPOSITE of 3 groups of 5 positives</u></p> 	$-15$
$-3 \times -5$			

# NOW YOU TRY: Solve $-2 \times 7$




<b>PROBLEM</b> 	<i>Write</i> 	 <b>Draw: Use integer tiles to represent the problem</b>	<b>The product</b>
$-2 \times 7$			






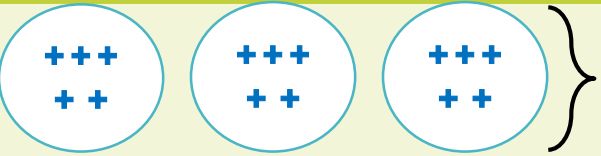
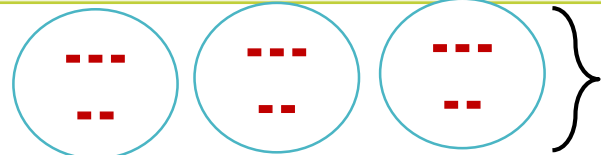
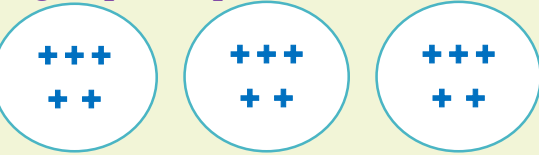


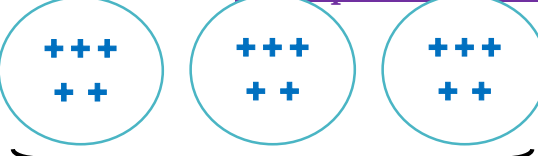
# Solve Problem 4: $-3 \times -5$

<b>PROBLEM</b> 	<i>Write</i> 	 <b>Draw: Use integer tiles to represent the problem</b>	<b>The product</b>
$3 \times 5$			
$3 \times -5$			
$-3 \times 5$			
$-3 \times -5$	<p>The <b>OPPOSITE</b> of 3 groups of 5 negatives</p>	<p><u>3 groups of 5 negatives</u></p>  <p>The total: <b>-15</b></p> <p>The <b>OPPOSITE</b> of 3 groups of 5 negatives</p> <p>The total: <b>15</b></p>	<p><b>15</b></p>

# NOW YOU TRY: Solve $-2 \times -7$

<b>PROBLEM</b> 	<i>Write</i> 	 <b>Draw: Use integer tiles to represent the problem</b>	<b>The product</b>
$-2 \times -7$			

# The 4 TYPICAL PROBLEMS of Multiplying Integers (COMPLETED)

<b>PROBLEM</b> 	<i>Write</i> 	 <b>Draw: Use integer tiles to represent the problem</b>	<b>The product</b>
$3 \times 5$	3 groups of 4 positives		<b>15</b>
$3 \times -5$	3 groups of 5 negatives		<b>-15</b>
$-3 \times 5$	The <b>OPPOSITE</b> of 3 groups of 5 positives	<p><u>3 groups of 5 positives</u></p>  <p>→</p> <p><u>The OPPOSITE of 3 groups of 5 positives</u></p> 	<b>-15</b>
$-3 \times -5$	The <b>OPPOSITE</b> of 3 groups of 5 negatives	<p><u>3 groups of 5 negatives</u></p>  <p>→</p> <p><u>The OPPOSITE of 3 groups of 5 negatives</u></p> 	<b>15</b>

# SIGN-OF-PRODUCT Table (*Incomplete*)

Signs of two integers <b>a</b> and <b>b</b>		Sign of the Product <b>a x b</b>
+	+	
+	-	
-	+	
-	-	



Thinking

# SIGN-OF-PRODUCT Table (Completed)

Signs of two integers <b>a</b> and <b>b</b>		Sign of the Product <b>a x b</b>
+	+	+
+	-	-
-	+	-
-	-	+



Thinking



## NOW YOU TRY: RULE of Signs in Multiplication

1. From the Sign-of-Product table, what do you notify about the signs of multiplication?

2. **Is there any rule of multiplication signs we can build up?**

- If two integers have the **same sign**, their product \_\_\_\_\_

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- If two integers have **different signs**, their product \_\_\_\_\_

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## NOW YOU TRY

Practice solving multiplication problems (Fill up the blanks)

$$-7 \times (-8) = \underline{\hspace{2cm}}$$

$$-4 \times 9 = \underline{\hspace{2cm}}$$

$$3 \times (-11) = \underline{\hspace{2cm}}$$

$$15 \times 19 = \underline{\hspace{2cm}}$$

$$4 \times (\underline{\hspace{2cm}}) = -4$$

$$\underline{\hspace{2cm}} \times -3 = 18$$

$$-9 \times (\underline{\hspace{2cm}}) = 45$$

$$\underline{\hspace{2cm}} \times 7 = -21$$

$$-5 \times 4 \times (-8) = \underline{\hspace{2cm}}$$

$$6 \times (-7) \times 3 = \underline{\hspace{2cm}}$$

$$-2 \times (-6) \times (-3) = \underline{\hspace{2cm}}$$